Experimental investigation of gamma stirling engine coupling to convert thermal to cooling energy in different laboratory conditions

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Abstract

The main aim of this research is to experimentally investigate the two coupled identical ST500 gamma-type Stirling engines and convert thermal energy to cooling energy. Using a new structure and two coupled Stirling engines at different temperatures and pressures and the use of biomass fuel within the 4-8 bar average pressure range of the first engine heat source, the 1-4 bar average pressure range of the second engine heat sink, and Stirling heat engine temperature range of 480-580 ºC, the effective cooling is obtained in the cooling engine. In doing tests, attempts were made to reach lower than 9 percent error results in different parts of the engine, including insulation, fluid leakage, belt loss, and measurement devices. According to the obtained results, 8 bars increase in the average pressure range of the gas in the first engine heat source, a 1 bar reduction in the average pressure range of the gas in the second engine heat sink, the increased temperature of the heat source up to 580ºC, and the use of the light operating fluid such as helium will affect the generation of cooling up to -16ºC.

Introduction

Stirling engine

Stirling engine is one of the heat air engines, in which the gas due to heating, tends to get expanded, and due to cooling, tends to get contracted, and this consecutive heating and cooling of the engine leads to movement of pistons and crank mechanism. Nowadays, different technologies for the development of using renewable energies are used. One of these technologies, which today is interesting is utilizing a heat engine called the Stirling engine [1]. Stirling engine is an external combustion engine and is highly flexible in terms of using different energy sources, and can convert the thermal energy in the renewable sources into mechanical and electrical energy [2].

Stirling motor is one of the heat air engines, which like other types of heat engines, by using heat exchange between a heat source and a cooling one, can produce mechanical and electrical work [3]. Heat enters the engine at a high temperature. Part of that converts to mechanical or electrical work and the rest is ejected from the motor at lower temperatures [4]. Stirling engine in terms of performance is simple and has good torque, and if used in reverse, it can be an alternative for the refrigeration cycles. Today, the introduction of new alloys and sealing materials, as well as the use of software and advanced computers that facilitate accurate and complex calculations, will accelerate the evolution of this engine. If optimization of the current engines for the reduction of fuel, emissions, and noise does not see the international standards of environmental organizations, without any hesitation we should go for Stirling engines [5].

Types of stirling engines

Stirling engines have been developed over the years and various designs of this type of engine have been developed.
Different types of Stirling engines are known as Alpha, Beta, Gamma, and Free Piston. The principles of thermodynamics are the same for all of them, and the main difference is in how the different components of the engine are placed next to each other.

All Stirling engines have five control volumes, which are compaction chamber, air conditioner, recovery, healing, and expansion chamber [6].

**Alpha type engine**

The Alpha engine has two separate cylinders for compression and expansion spaces, and a piston in each cylinder. Two separate cylinders are connected by a heat sink and an interface pipe. The heating cylinder is placed next to the heat source and the cooling cylinder is placed next to the heat sink. These types of engines are conceptually the simplest configuration of Stirling engines. In the alpha engine, the volume of each of the engine’s heat and cooling chambers is determined using the heat and cooling pistons, whose motion is controlled, respectively. Figure 1 shows the schematic of the Stirling engine with alpha structure along with the heat inlet and its heat sink, in which the movement of the pistons is controlled by the rotation of the crankshaft and the four processes expressed in every 90 degrees of rotation of the crankshaft. To be. In this method, both heat and cooling pistons need to be sealed; This may not be a problem for the cooling side piston, but complete sealing of the heat side piston due to the different thermal expansion coefficients of the piston and cylinder wall will be a problem, which is one of the design complexities of this structure [7].

**Beta type engine**

Robert Stirling was invented as the first and oldest Stirling engine with a beta structure. In a beta engine, the heat side piston is removed and replaced by a cylindrical piece called a displacer between the heat and cooling chambers. In this case, due to the removal of the heated piston, the sealing problem around the piston disappears [8]. A schematic of the beta-type Stirling engine is shown in Figure 2.

**Gamma type engine**

The Gamma-type Stirling engine is structurally similar to the beta engine, except that the piston is located in a separate cylinder relative to the displacement. The Gamma Stirling engine has a lower compression ratio than the Alpha and Beta models, but because only its power piston needs to be sealed and the cylinders are separate, it has the simplest mechanical arrangement among other Stirling engines [9]. A schematic of a gamma-type Stirling engine is shown in Figure 3.

**Free piston engine**

This type of engine produces power from the reciprocating motion of the piston and does not actually require a flywheel or crankshaft; For this reason, they do not have problems with balance and bearing or bearing failure. In addition, due to its smaller volume and weight than other types, it is easier to install them in different places such as solar dishes. Due to the lack of flywheels in open-piston engines, they use a plate spring or oscillating beam to reverse the piston or to connect several free-piston engines to each other as shown in Figure 4 [10].

In the field of analysis and modeling of the Stirling engine, Schmidt [11] performed the first thermodynamic analysis. In this model, the temperature of the compaction chamber with...
saving energy consumption, reducing emissions, and saving for four different climates of Iran with the help of three goals, stroke simultaneous production system with the Stirling engine in a laboratory and numerical manner. And electricity with the primary actuator of the Stirling beta and Sheikhi [23], studied the simultaneous modeling of heating and cooling with respect to construction and air pollution by reducing NOX and CO2, CO showed leakage of this system at low pressures to a lesser extent. Francisco Callis, et al. [25], performed the optimization strategy of a combined cooling, heat, and power system for an engine in precise numerical analysis and found that the system’s optimal capacity was less than the actual design.

L. Brin, et al. [26] examined the overall performance of the refrigerator for the Stirling pair heat engine and the amount of work related to the final cooling with respect to construction effects and parameters such as temperature ratio for the engine and its density. Ansari Nasab, et al. [27]. Combined the Stirling engine with a molten carbonate fuel cell, and a gas turbine for simultaneous production of electricity, heating, and cooling, examined the sensitivity, and finally proposed three strategies to eliminate unnecessary costs that have improved system performance. Dai, et al. [28] investigated the Stirling engine process using the finite–time thermodynamics and the hypothesis of uniform temperature distribution, analysis, and the effect of various parameters and their limitations.

Figure 4: Schematic of free-piston type Stirling engine.
Katoli, et al. [29] simulated and experimentally evaluated a Stirling refrigerator unit to convert electrical–mechanical energy into cooling energy experimentally and the effects of fluid pressure and alternator power for cooling. Sowale, et al. [30] have experimentally investigated a single gamma–type Stirling engine for cooling production using different gases. The results were obtained at a temperature of about -23 °C using the working fluid of the air and at a temperature of about -21 °C with helium gas. The results showed that increasing the power of the power supply, medium gas pressure, time of turning on the power supply, and the use of light operating fluid such as air, helium will be effective in producing cooling.

This research is written from a single gamma–type Stirling engine and the use of a power supply to generate cooling, which is experimentally used in a new structure using a couple of ST500 gamma–type Stirling engines and energy conversion. Heat to mechanical energy to produce cooling by helium operating fluid in the medium pressure range of the first engine heat source 4 to 8 times and the average heat sink pressure range of the second engine 1 to 4 times and the temperature range of the Stirling heat engine 480 to 580 °C can be cooled effectively on the cooling engine. The start of the first Stirling engine was performed experimentally using the combustion of biomass resources and the heat from the combustion of agricultural materials and wastes was transferred to the first Stirling engine and the engine started and started the second Stirling engine and produced cooling. Cooling below zero degrees Celsius can be achieved by increasing the thermal energy to 580 °C and increasing the supply pressure of the heat Stirling engine fluid by up to 8 times and decreasing the supply pressure of the cooling engine fluid by up to 1 time. Generating cooling from renewable sources, in addition to environmental impacts, also makes the future of energy safer. According to the research, the production of cooling was a new method and it has not been done yet with less error and more accuracy, more accurate results were obtained in a laboratory sample of Stirling ST500 type gamma motor, for cooling application in various industries, Automotive is recommended.

In summary, the objectives of this research were to design and build a heat chamber with biomass fuel for high-temperature sources and mechanical power generation by the first Stirling engine and finally to produce cooling by the second Stirling engine. During the experiments, the values of temperature, efficiency, power, and pressure due to different temperatures in heating and cooling of the Stirling Gamma ST500 engine were measured using a test engine reader and Adam software and the results were compared with previous research, comparison and validation based on Nlog code are done.

**Methodology**

**Theoretical modelling**

**Nlog code:** The Nlog code is written by the MATLAB program and is used for thermodynamic analysis of the Stirling engine, and is a Stirling engine cycle analysis code that uses third–order equations. This code calculates the heat output and output power of the Stirling engine.

Geometric characteristics of all gas transmission channels, pipes, and expansion chambers and density Geometry of connections between the moving parts of the engine and initial pressure of the engine and the initial temperatures at any point of the heat exchanger wall temperature which is considered constant over time. Nlog code divides all gas channels and pipes in the engine into control volumes and divides the dynamics and thermodynamic parameters for each control volume by solving continuity equations, momentum, and determined energy. Using this structure, cooling can be generated directly from heat from renewable or non–renewable sources. The results obtained for the production of cooling were compared using the Nlog code previously validated by the authors in valid articles [19,20].

**Mathematical modeling**

In this research, a third–order thermodynamic dynamic model is used, which can be used to estimate the instantaneous speed of the engine in terms of time by estimating the variables of the operating fluid state of the engine and to estimate the final efficiency and power output of the engine. In this dynamic–thermodynamic model, first, the various chambers of the Stirling engine, including heating, cooling, recovery, etc. in the form of volume – control with heat exchange, work, and mass with its environment and also with the volume – controls Are considered adjacent. Heat transfer surface, heat transfer coefficients, and thermal conductivity are effective in both heat receiving and dissipation processes. The thermal conductivity is much larger than the displacement heat transfer coefficient and therefore the resistance conduction heat was discarded and only heat transfer was considered as a limiting factor for heat absorption and dissipation. Regarding the recovery, the limitation of the thermal conductivity of the recovery is ignored. In order to investigate the effect of pressure drop due to fluid motion, the fluid pressure at all points of each volume–control is considered the same and different from adjacent sections. Having the geometry, dynamic characteristics, and wall temperature of heat and cooling heat sources for the engine, fluid pressure drop coefficient and heat transfer coefficients are calculated through experimental relationships.

**Thermodynamic relations**

The principles of thermodynamics are the same for all Stirling engine structures, and there is a fundamental difference in how the various components are placed next to each other [31].

\[
q = RT \ln r = \frac{P}{V} \ln r
\]

\[
w = R(T_b - T_c) \ln r
\]

\[
\eta = \frac{w}{q} = \left(1 - \frac{T}{T_b}\right)
\]

In the above relations, \( q \) is the amount of heat received and \( w \) is the productive work in joules (J) in an ideal Stirling cycle. The heat sink in Kelvin (K) is the ratio of engine density,
which is the ratio of the maximum volume of the system to its minimum volume, $P_i$, $V$, and the pressure and volume in Pascal and cubic meters, respectively.

**Dynamic relationships governing the model**

In this research, a thermodynamic dynamic model that was previously written and validated for the heating mode of the Stirling engine was used [19]. One of the advantages of using the Stirling engine is the ability to reverse the duty cycle; Therefore, by changing the code pattern, it can be used to generate cooling. Validation of cooling code and cooling products in the laboratory using two Stirling ST500 engines of gamma type in research and development company Iran Khodro was performed experimentally for the first time and the results were analyzed. The kinematic parameters of the engine are shown in Figure 5.

Parameters of $\theta$, $C_1$, $C_2$, $d$, $l_1$, $l_2$, $r_c$, and $a_1$ to $a_3$ are structural parameters of the engine and have a fixed value. Equations 2 and 3 relate these parameters to $b_1$ and $b_2$ (the vertical distance of the Gajn pin at any moment to the direction of the crankshaft).

$$L_1 = r_c^2 + b_1^2 + 2r_c b_1 \cos(\theta)$$  \hspace{1cm} (2)

$$L_2 = r_c^2 + b_2^2 + 2r_c b_2 \cos(\theta + \varphi)$$  \hspace{1cm} (3)

By solving the above equations for $b_1, b_2$, they are expressed as functions of the crank angle shown in Equations 4 and 5 [32].

$$b_1 = (r_c^2 \cos^2 \theta + L_1^2 - r_c^2)^{\frac{1}{2}} - r_c \cos \theta$$  \hspace{1cm} (4)

$$b_2 = \frac{r_c^2 \cos(2\varphi + 2\theta)}{2} + L_2^2 - \frac{r_c^2}{2} + r_c \cos(\varphi + \theta)$$  \hspace{1cm} (5)

Therefore $x$ (length of compaction chamber), $x$ (length of heat chamber) and $x$ (length of cooling chamber) are obtained in terms of the crankshaft angle shown in Equations 6 to 8.

$$x_1 = c_1 - a_1 - b_1$$  \hspace{1cm} (6)

$$x_2 = c_2 - a_2 - b_2$$  \hspace{1cm} (7)

$$x_3 = d - a_3 - x_2$$  \hspace{1cm} (8)

The derivatives of $x$, $x$, relative to the crankshaft angle are also shown in Equations 9 and 10. These relations will be used in the dynamic relations calculation section.

$$\frac{dx_1}{d\theta} = \frac{r_c^2 \sin(2\theta)}{2(L_1^2 - r_c^2 \sin^2 \theta)^{\frac{1}{2}}} - r_c \sin(\theta)$$  \hspace{1cm} (9)

$$\frac{dx_2}{d\theta} = \frac{r_c^2 \sin(2\varphi + 2\theta)}{2(L_2^2 - r_c^2 \cos^2 (2\varphi + 2\theta))^2} + \frac{r_c^2}{2} - r_c \sin(\varphi + \theta)$$  \hspace{1cm} (10)

The first derivatives $x_1, x_2$ which represent the velocity of the moving parts of the engine, are calculated using equations 11 and 12, and the second derivatives, which represent their acceleration, are calculated from equations 13 and 14 according to the rules of chain derivatives.

$$\frac{dx_1}{dt} = \frac{dx_1}{d\theta} \frac{d\theta}{dt}$$  \hspace{1cm} (11)

$$\frac{dx_2}{dt} = \frac{dx_2}{d\theta} \frac{d\theta}{dt}$$  \hspace{1cm} (12)

$$\frac{\delta^2 x_1}{\delta t^2} = \frac{\delta x_1}{\delta \theta} \frac{\delta \theta}{\delta t}$$  \hspace{1cm} (13)

$$\frac{\delta^2 x_2}{\delta t^2} = \frac{\delta x_2}{\delta \theta} \frac{\delta \theta}{\delta t}$$  \hspace{1cm} (14)

**Model of kinetics relationships**

First, we have to find a differential equation that solves the speed and angle of the crankshaft moments and for this purpose the Lagrange dynamic method is used. The general form of Lagrange equations is shown in Equations 15 to 18. The sum will be $V_\theta$ and the sum of the potential energies of the components in the variable $T_\theta$. The kinetic energies of all the moving parts of the motor will be included in the variable. Lagrange is obtained by subtracting the total kinetic energy from the total potential energy, and finally, by placing the Lagrange in the principal Lagrange equation (Equation 18) and the necessary derivatives, the dynamic differential equation of the Stirling engine is obtained. The in the Lagrange equation represents the amount of equivalent torque applied.
to the engine crankshaft, while $I$ represents the variable of the crankshaft angle [33].

$$T_\theta = \sum_{i=1}^{2} \frac{1}{n_i} m_i x_i + \sum_{i=2}^{2} \frac{1}{2} j_{ii} \theta_i$$

(15)

$$V_\theta = \sum_{i=1}^{2} \frac{1}{2} k_i x_i^2$$

(16)

$$L_\theta = T_\theta - V_\theta = \sum_{i=1}^{2} \frac{1}{n_i} m_i x_i + \sum_{i=2}^{2} \frac{1}{2} j_{ii} \theta_i - \sum_{i=2}^{2} \frac{1}{2} k_i x_i^2$$

(17)

$$\frac{d}{dt} \left( \frac{\partial L_\theta}{\partial \dot{\theta}} \right) - \frac{\partial L_\theta}{\partial \theta} = I_c$$

(18)

According to the number of variables considered, Lagrangian is obtained as Equation 19.

$$L_\theta = \frac{1}{2} \theta \left( m_1 \left( \frac{dx_1}{d\theta} \right)^2 + m_2 \left( \frac{dx_2}{d\theta} \right)^2 + J_c \right)$$

(19)

By placing the relations 11 and 12 in Equation 19, Equation 20 is obtained.

$$L_\theta = \frac{1}{2} \theta \left( m_1 \left( \frac{dx_1}{d\theta} \right)^2 + m_2 \left( \frac{dx_2}{d\theta} \right)^2 + J_c \right)$$

(20)

The calculated derivatives in Equations 9 and 10 are placed in Equation 20, and Lagrangin is obtained in terms of crankshaft angle and crankshaft angle velocity according to Equation 21.

$$L_\theta = \frac{1}{2} \theta \left( m_1 \left( \frac{r_c^2 \sin(2\theta)}{2} - r_c \sin(\theta) \right)^2 + m_2 \left( \frac{r_c^2 \sin(2\phi + 2\theta)}{2} - \frac{r_c}{2} \sin(\phi + \theta) \right)^2 + J \right)$$

(21)

Therefore, if the derivatives of the Lagrange equation are applied to the Lagrangin, one unit is added to the degree of the derivative in the equations and the left part of the Lagrange equation becomes a function of angle, velocity and acceleration of the crankshaft to the form of Equation 22.

$$\frac{d}{dt} \left( \frac{\partial L_\theta}{\partial \dot{\theta}} \right) - \frac{\partial L_\theta}{\partial \theta} = f(\theta, \dot{\theta}, \ddot{\theta})$$

(22)

Experimental modelling

The stirling engine used in this research: The studies performed in this study were performed on the ST-500 engine available at the Iran Khodro Engine Research Center (or Peko), the technical specifications of which are shown in Table 1. The exterior of the engine is shown in Figure 6. In the form of the main parts of the engine, including the heater, cooler, exhaust, flywheel and piston housing are discarded [19].

Some parts of the Stirling engine such as heaters, water coolers and coolers can be seen in Figures 7,8.

Influential parameters in the experiment

1. Geometric characteristics of gas transmission channels, pipes and expansion and compression guards
2. Geometry of connections between moving parts of the engine
3. Initial engine pressure and initial temperature anywhere

Table 1: Stirling engine ST500 specifications.

<table>
<thead>
<tr>
<th>36. Quantities (unit)</th>
<th>Technical characteristics</th>
</tr>
</thead>
<tbody>
<tr>
<td>500 (w)</td>
<td>Output power</td>
</tr>
<tr>
<td>8.5 (%)</td>
<td>Thermal efficiency</td>
</tr>
<tr>
<td>8 (bar)</td>
<td>Standard charge pressure</td>
</tr>
<tr>
<td>air, Helium</td>
<td>Working fluid</td>
</tr>
<tr>
<td>14 (hertz)</td>
<td>Working frequency</td>
</tr>
<tr>
<td>water</td>
<td>Coolant</td>
</tr>
<tr>
<td>0.075 (m)</td>
<td>Piston range of motion</td>
</tr>
<tr>
<td>0.075 (m)</td>
<td>Gas displacer range of motion</td>
</tr>
<tr>
<td>90 (degree)</td>
<td>Phase angle</td>
</tr>
<tr>
<td>20*6 (mm)</td>
<td>Heaters type</td>
</tr>
<tr>
<td>channel 144*13 (mm)</td>
<td>Cooler type</td>
</tr>
<tr>
<td>0.96</td>
<td>Material of recovery</td>
</tr>
<tr>
<td>350-420 (C)</td>
<td>Heat absorption temperature</td>
</tr>
<tr>
<td>30-50 (C)</td>
<td>Heat dissipation temperature</td>
</tr>
<tr>
<td>3-10*1.79 (m)</td>
<td>Maximum volume</td>
</tr>
<tr>
<td>3-10*1.39 (m)</td>
<td>Minimum volume</td>
</tr>
<tr>
<td>1.3:1</td>
<td>Density ratio</td>
</tr>
</tbody>
</table>

Figure 6: Exterior view of Stirling engine ST-500.
in the engine
4. Heat exchanger wall temperature
5. Gas used in heat and heat sink
6. Material of regenerative

Specifications of the regenerative used in the Stirling engine are shown in Table 2. In the tests, the air pressure of the operating fluid is 6 times and the generating power is considered to be a constant 420 watts. The voltage and current of the power supply are equal to 20 volts and 21 amps, respectively, and the ambient temperature in all the experiments is constant and equal to 25°C.

**Measure the belt loss before the test**

In order to be accurate in the tests, the losses in the belt must be measured. The belt is used to transfer power from the heat engine to the cooling engine, and if the loss rate is more than a certain limit, the test error increases and the results are not reliable. For this reason, the losses in the belt should not exceed the specified limit.

The specifications of the heat engine, alternator and Stirling engine flywheels along with their period are given in Table 3.

As can be seen from the experimental results in Table 3, the belt error percentage is less than 9% and therefore it can be said that the existing belt has a good power transmission [30].

**Test steps**

The experiments were performed in the following three steps:

1. Evaluation of the results of a single Stirling motor for cooling production using an air-powered fluid power supply at 520.8 watts and a working pressure of 3 times in 10 minutes
2. Evaluation of the results of a single Stirling engine for cooling production using a power supply with helium gas at a capacity of 420 watts and a working pressure of 6 times in 10 minutes and validation with previous research
3. Experimental study of coupling Stirling engine for cooling production by receiving heat energy from heat source for the power of the first Stirling engine and generating cooling with the second Stirling engine using helium operating fluid and validation by previous research.

**Test for air-cooled cooling engine**

Figure 9 Schematic of Gamma Stirling engine for cooling production. In Figure 10, the alternator was connected to a power supply (generator) and used for the initial release of the motor. The alternator was also connected to the flywheel using a belt. When the power supply is turned on, the alternator rotates and power is transmitted to the flywheel by a belt. In this case, according to the stirling cycle, the heating part of the device cools down and the temperature drops below zero degrees after a few short minutes. Copper pipes have been used to measure the heat transfer of the cooling section. To measure the amount of heat transfer, water first flows into the copper pipes by a pump. The effluent was then collected in an insulated chamber. By measuring the water discharge from the copper pipes as well as measuring the temperature of the inlet and outlet water of the copper pipes, the amount of heat transfer in the heating section of the device was obtained according to Formula 23.

![Figure 7: Stirling engine heater with recovery.](https://www.peertechzpublications.com/journals/global-journal-of-biotechnology-and-biomaterial-science/

![Figure 8: Stirling engine coolant and fluid passage ducts.](https://www.peertechzpublications.com/journals/global-journal-of-biotechnology-and-biomaterial-science/

![Table 2: Specifications of the regenerative used in the Stirling engine [34].](https://www.peertechzpublications.com/journals/global-journal-of-biotechnology-and-biomaterial-science/

<table>
<thead>
<tr>
<th>Specification</th>
<th>Copper</th>
<th>Pure Iron</th>
<th>Carbon steel</th>
<th>Aluminium T6-2024</th>
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</thead>
<tbody>
<tr>
<td>Density (kg/m³)</td>
<td>8920</td>
<td>7870</td>
<td>7854</td>
<td>2770</td>
</tr>
<tr>
<td>Heat capacity (J/kg K)</td>
<td>385</td>
<td>447</td>
<td>434</td>
<td>875</td>
</tr>
<tr>
<td>Conductive heat transfer coefficient (W/m K)</td>
<td>390</td>
<td>80.2</td>
<td>60.5</td>
<td>177</td>
</tr>
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</table>

![Table 3: Specifications of alternator and two Stirling engines.](https://www.peertechzpublications.com/journals/global-journal-of-biotechnology-and-biomaterial-science/

<table>
<thead>
<tr>
<th>Heater motor specifications</th>
<th>Cooler motor specifications</th>
<th>Dynamo specifications</th>
</tr>
</thead>
<tbody>
<tr>
<td>D1 (mm) 280</td>
<td>D2 (mm) 258</td>
<td>D (mm) 258</td>
</tr>
<tr>
<td>N1 (rpm) 250</td>
<td>N2 (rpm) 386</td>
<td>N (rpm) 1350</td>
</tr>
<tr>
<td>N1d1 70000</td>
<td>N2d2 73788</td>
<td>Nd 681175</td>
</tr>
</tbody>
</table>
The actual view of the Stirling Gamma engine with insulation is shown in Figure 11.

Initially, the Stirling engine was started using a power supply in laboratory conditions at different power, pressure and temperatures. For accuracy in experiments, ambient temperature, discharge water discharge from copper pipes were considered constant and equal, and for better comparison of results, the input power was confirmed by the alternator power supply in each experiment. In order to examine and compare more accurately, experiments were performed for different time intervals at different pressures, power and gases, and the production cooling temperature was calculated at each stage.

Table 4 does not show the initial conditions for the four different experiments performed on the Stirling engine to generate cooling using air gas. In these experiments, the air pressure of the operating fluid was 3 times and the dynamo power was considered to be constant 520.8. Experiments 1, 2, 3, and 4 were performed over a period of 2 to 10 minutes. For all four flow tests, the discharge of water out of copper pipes was considered constant and equal. To better compare the results, the input power was fixed by the power supply. The voltage and current of the power supply were 31 volts and 17 amps, respectively, and the ambient temperature in all four experiments was constant and the temperature was T4, T and 25 °C. The temperature of the inlet and outlet parts of the copper pipes at the top and bottom of the cooling part of the temperature reader T was measured. Finally, with increasing dynamo power and gas pressure, the temperature of 1 T of the cooling produced reached about -23 degrees Celsius.

Test for cooling engine using helium gas

Table 5 shows the initial conditions for the four different experiments performed on the Stirling engine to generate cooling using helium gas. In these experiments, the pressure of the working fluid was 6 times, the power of the alternator was 420 watts at 3 and 4 times for 2 to 10 minutes. For each of the discharge tests, the water discharge from the copper pipes was considered constant and equal to 2. To better compare the results, the input power was fixed by the power supply. The voltage and current of the power supply were equal to 20 volts and 21 amps, respectively, and the ambient temperature in all four experiments was constant and equal to 25 degrees Celsius. According to Figure 9, the temperature of the inlet and outlet increasing the power of the alternator and gas pressure, the temperature of the cooling part T1 of the Stirling engine will reach about -23 degrees Celsius.

Test for cooling engine using helium gas

Table 5 shows the initial conditions for the four different experiments performed on the Stirling engine to generate cooling using helium gas. In these experiments, the pressure of the working fluid was 6 times, the power of the alternator was 420 watts at 3 and 4 times for 2 to 10 minutes. For each of the discharge tests, the water discharge from the copper pipes was considered constant and equal to 2. To better compare the results, the input power was fixed by the power supply. The voltage and current of the power supply were equal to 20 volts and 21 amps, respectively, and the ambient temperature in all four experiments was constant and equal to 25 degrees Celsius. According to Figure 9, the temperature of the inlet and outlet
parts of copper pipes at the top and bottom (T 4, T 5) and the production cooling temperature of 1 T are measured by the temperature reader and finally reach about -21°C.

Table 6 shows the properties of the operating fluids used at temperatures of 0°C. Gases that are less viscous will have more exhaust power under similar operating conditions.

In Figure 15 experiments at 3 bar pressure and power of 441.14 to 476 watts have been done and using gamma stirling motor and helium operating fluid the cooling is done. The aim is to evaluate and repeat the tests and validate them.

Figure 16 shows the temperature-time diagram for the four experiments. As shown, when the power supply is turned on, the temperature of the heater's unit decreases until the power supply motor is switched off. Finally, after a certain period of time, increasing the dynamo power and gas pressure, the temperature of the cooling part of the Stirling engine will be as shown in Figure 11 and the temperature of the head part (T 1) has reached about -21 degrees Celsius [29] was validated and more accurate results and graphs were obtained with further experiments. Helium tank for operating fluid source pressure is shown in Figure 17.

**Measuring the power consumption of a heat engine individually using a heat burner**

Figure 18 shows the alternator in Stirling engine and heat chamber. First, the heat engine was started individually to measure the power consumption when a heat flame is used. The release of this motor is such that it was first started using the motor power supply and then the Stirling motor started to rotate and over time, its rotation increases. In this case, the current and voltage consumption of the motor were 4.6 amps and 31 volts, respectively; Therefore, the power consumption of a single heat engine can be obtained as follows:

\[ W_{\text{Hot motor}} = VI = 31 \times 4.6 = 142.6 \text{ Watts} \]  

(25)

**System’s input power while using the biogas burner**

As it is clear in Table 7, the biogas is mostly comprised of methane and reaches to a temperature of 500º C. At this temperature, the gases H2S and CH4 reach their ignition temperatures and the heat within them is released. It is noteworthy to mention that the ignition temperature of 1 Hydrogen sulfide equals to 232º C [36]. The ignition
temperature of other gases within the biogas is higher than the operating temperature in this study. Methane combustion reaction equation is as follows [37]:

\[
\text{CH}_4 + 2\text{O}_2 \rightarrow \text{CO}_2 + 2\text{H}_2\text{O (l)}
\]

The thermal value of methane combustion is 34.83 Megajoule/m³. The urban gas flow used in this research has been calculated to be 25 lit/min using a flow meter. Therefore, the input power to the system can be calculated through the total heat resulting from urban gas combustion. Urban gas flow meter device is shown in Figure 19.

\[
Q = m \times C_v = 25 \text{lit} / \text{min} \times 34.83 \text{MJ/m}^3
\]

\[
\text{lit} / \text{m} = 14.5 \text{KJ} / \text{s} = 14.5 \text{KW}
\]

Hydrogen sulfide combustion reaction equation will be as follows:

\[
2\text{H}_2\text{S} + 3\text{O}_2 \rightarrow 2\text{SO}_2 + 2\text{H}_2\text{O}
\]

The thermal value of the combustion of Hydrogen sulfide is 36.503 Megajoule/m³. As this gas comprises about 0.2% of the biogas, it should be said that the input power resulting from the combustion of this gas can be described using the below equation:

\[
\text{min} \times 1 \text{min} \times 60 \times 1 \text{m}^3 \times 1000 \text{l} \times 36.503 \text{MJ/m}^3
\]

\[
\times 0.002 = 3.04 \times 10^{-5} \text{KW} = 0.0304 \text{W} / 25
\]

Therefore, it can be argued that, the input value resulting...
from the combustion of Hydrogen sulfide is very negligible compared with that of Methane. The reason behind it is that Hydrogen sulfide has a small share within the biogas. Therefore, the biogas could be considered against Methane with a good approximation.

The gas burner is responsible to maintain the temperature in the heat part of the engine while, water with a stabilized temperature is in charge of maintaining the temperature in the cooling part of the motor (engine). Gas and water flow has been adjusted manually so as to bring about the necessary conditions for engine's performance in its stable state. Since the variables are sufficiently stable in this state, using an automatic controller to adjust the gas and water flow may not be needed. Temperature sensors of thermocouple type have been used (as shown in Figure 20) to read the temperature of water in the inlet and outlet cooling parts of the motor as well as the temperature in two points of motor’s heating pipes.

**Third stage: The conditions of testing the Stirling engine coupling for cooling generation using a power supply and Helium gas**

Figure 21 illustrates the schematic belonging to the coupling of Stirling engine. The left side is named heat engine which operates by receiving thermal energy from a heat source like biomass. In the right side, another Stirling engine can be seen which is named the cooling engine. This engine generates cooling by receiving energy from the heat engine. This system includes two Stirling engines. The initial setup of the first engine requires a power supply and a generator which connect to the flywheel of the first engine. A few seconds after the setup, the generator can be disconnected so that the system can continue its operation. After launching the first engine, the second one will be started through the belt. According to the cycle of the Stirling engine, the rotation of the second engine will produce cooling. The first Stirling engine, the heat one, and the second Stirling engine are named the cooling Stirling engine.

As for the engines to operate, it is needed that the two engines be coupled to one another. As illustrated in the figure below, a special insulation will be used in the heating part of the cooling engine so as to avoid cooling energy wastes. Each of the two engines will be filled with Helium gas. In this part, care should be taken that the gas pressure of the heat engine be higher than that of the cooling engine so that the system will run more easily, because the average gas pressure of the heat and cooling supplies is one of the most important factors of the experiment. One of the characteristics of Stirling engine is its requirement to be preheated before any use; therefore, in this study, urban gas will be used to heat the engine. A burner is used to preheat the engine for 5 minutes. The real representation of Stirling engine coupling ST500 (heat and cooling) to generate cooling, heat burner of Stirling engine and heat engine's temperature sensor and engine’s output reader device and Adams software are shown in Figures 22-24 respectively.

**Results and discussion**

**Test results of the coupling of the two engines to produce cooling**

Table 8. demonstrates the initial conditions for 5 various tests done on the couple Stirling engine to produce cooling using Helium gas. In this experiment, the pressure of the Helium operating fluid is at best 8 bars in the heating source and the average pressure in the cooling source is 1 bar. Tests 1–5 have been carried out in a timespan of 2–4 minutes. For each of the
five tests, the discharge water fluid from the copper coils has been considered as fixed. For a more precise comparison of the results, the input power from the power supply is considered stable. The ambient temperature in all five tests is 25°C. The temperature of the generated cooling (T5) is measured by a temperature reader device.

Figure 25 illustrates the temperature-time diagram of the 5 so-called experiments. As it is shown, when the pressure of the heat and heat sinks changes, the temperature of the heating part rises and that of the cooling part of the device decreases and consequently cooling is produced. Eventually, by making use of a new experimental design which involves incorporating two Stirling engines in varying temperature and pressure conditions as well as the presence of a biomass fuel, the average pressure of the heating/heat source increased by 8 bars and the cooling/source temperature decreased by 1 bar; this in turn caused the temperature of the cooling part to (T5) reach to −16°C.

Test results of the coupling of the two engines to produce cooling by the use of the Nlog code

As stated previously, the Nlog code is written using MATLAB software and it is used for the thermodynamic analysis of the Stirling engine. Nlog is an analysis code of Stirling engine’s cycle within which cubic equations are used. This code calculates the output heat and the power output of Stirling engine. By using this design, cooling can be generated directly from the heat produced by renewable or non-renewable sources of energy. The obtained results for cooling generation using Nlog have been compared with the results previously obtained and validated by other researchers [13]. The P-V diagram is shown in Figure 26.

Table 8: Different laboratory conditions for the couple Stirling engine to produce cooling.

<table>
<thead>
<tr>
<th>Test No</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Duration of the power supply on-time (mins)</td>
<td>2</td>
<td>3</td>
<td>3</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>the average gas pressure of the heat source / heating source (bars)</td>
<td>8</td>
<td>6</td>
<td>6</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>The average gas pressure of the could source/ cooling source (bars)</td>
<td>1</td>
<td>3</td>
<td>4</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>Ambient temperature (ºC)</td>
<td>28</td>
<td>26</td>
<td>27</td>
<td>30</td>
<td>25</td>
</tr>
<tr>
<td>The final temperature of the heat engine (ºC)</td>
<td>580</td>
<td>520</td>
<td>490</td>
<td>510</td>
<td>480</td>
</tr>
<tr>
<td>The initial primary temperature of the cooling/ cooling engine (ºC)</td>
<td>24</td>
<td>23</td>
<td>24</td>
<td>27</td>
<td>23</td>
</tr>
<tr>
<td>The final temperature of the coolin/ cooling engine (ºC)</td>
<td>-16</td>
<td>-12</td>
<td>-8</td>
<td>-15</td>
<td>-12</td>
</tr>
<tr>
<td>The operating fluid</td>
<td>Helium</td>
<td>Helium</td>
<td>Helium</td>
<td>Helium</td>
<td>Helium</td>
</tr>
</tbody>
</table>

As can be seen in the P-V diagram, according to the Nlog output, the black diagram represents the Schmidt mode, the blue one belongs to the cooler (the second Stirling engine), and the red one is for the heating (the first Stirling engine) and that they have a fine conformity. Using two Stirling engines in a coupled mode has a high efficiency in both thermal and electrical terms. Therefore, using the Stirling engine so as to produce cooling can be a suitable option. For instance, it can be used to produce cooling in both home and industrial sectors. Producing low levels of noise and vibration, and their capability of being built in small scales are among the advantages of Stirling engines in cooling mode.

Conclusion

In this study, two Stirling and coupling motors were investigated and a heat source was used for the high temperature source of the first Stirling engine. The output of the first Stirling engine moved the second Stirling engine to create a second cooling Stirling engine. Optimization and production of cooling using biomass fuel in vitro using two Gamma type was performed for the first time in Iran Khodro Research and Development Center (Ipco Company) and the results of Stirling ST500 engine were analyzed. The results of this research can be used for the development of Stirling engines in the world and sustainable development, which have
been important issues today, using the laboratory method and coupling of Stirling engines, as well as the use of renewable fuels. Finally, Stirling motors are used to apply cooling at pressures of different periodic temperatures. In this research, by using a new coupling structure of Gamma Stirling engine and by designing and constructing a heat chamber that works with biomass fuel, the mechanical power of the first Stirling engine can be increased.

Produced to cool at medium pressure, heat engine gas 8 times, average cooling engine pressure 1 time and the final temperature of the first Stirling heat engine at $580^\circ\text{C}$ to cool in the second Stirling cooling engine at $-16^\circ\text{C}$. With a careful design, select and increase the operating fluid pressure in the heat Stirling engine and reduce the average gas pressure in the heat sink. The high heat output of the heat Stirling engine causes the temperature in the cooling Stirling engine to decrease and it turns into a refrigerator. Heavier gases can also be used in Stirling engines, but these gases are less efficient than lighter gases such as helium and hydrogen. Smaller model engines also use air, but no other gas up to this level is used except in experimental cases.

Theoretically, the use of a light gas such as hydrogen or helium as the working fluid is recommended due to its low viscosity and high heat transfer coefficient. However, low molecular weight means an increase in the rate of fluid leakage from the engine, and as a result of the pressure drop, the efficiency of the increase in costs (fluid recharging) will decrease; High heat exchanger temperatures can cause parts to oxidize and corrode. In short, a gas can be selected as the optimal operating fluid, which in addition to being light, has a high heat transfer coefficient, low viscosity coefficient, low leakage potential and no oxidizing properties. In addition to the gases mentioned as working fluids, the researchers used gases such as carbon dioxide, water vapor and chemical composites.

References


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